# n-Octadecane: A Correction and Refinement of the Structure given by Hayashida 

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#### Abstract

Owing to a mis-indexing of the 0 kl zone, the triclinic cell proposed by Hayashida (J. Phys. Soc. Japan (1962), 17, 306) for octadecane, $\mathrm{C}_{18} \mathrm{H}_{38}$, is not correct : nor therefore is the structure proposed by him. The error has been corrected and the structure refined from Hayashida's $h 0 l$ and $0 k l$ data. Even after correction, the structure showed some minor anomalies. These we believe are due to inaccuracies in Hayashida's triclinic cell parameters. Good results are obtained using the cell originally proposed by Müller \& Lonsdale (Acta Cryst. (1948), 1, 127), suitably transformed to suit the axial system used by Hayashida, namely, $a=4 \cdot 28_{\mathrm{s}}, b=4 \cdot 82_{0}, c=24 \cdot 89_{8} \AA, \alpha=85 \cdot 15_{0}, \beta=67 \cdot 8$ and $\gamma=72 \cdot 7_{0}{ }^{\circ}$. Space group $P \overline{1}$.


If sufficiently pure, the straight chain alkanes $\mathrm{C}_{n} \mathrm{H}_{2 n+2}$ with $n$ even ( $6<n<26$ ) crystallize in the triclinic system (a hexagonal form is exhibited near the m.p.), whereas those with $n$ odd $(11<n<43)$ are orthorhombic (Broadhurst, 1962). A representative structure of the $n$ odd has been given for $\mathrm{C}_{23} \mathrm{H}_{48}$ by Smith (1953). For so simple a molecule the structure analysis of octadecane has had a chequered history.

The first single-crystal examination of $\mathrm{C}_{18} \mathrm{H}_{38}$ seems to have been that of Müller \& Lonsdale (1948), hereafter M \& L. They determined the six parameters for the triclinic cell (I, Table 1), showing it to contain one molecule. Kitaigorodsky \& Mnyukh (1959) obtained from Lonsdale $h 0 l$ and 0 kl intensity data which had apparently been recorded but not referred to in the 1948 paper with Müller. From these intensity data, Kitaigorodsky \& Mnyukh proposed an approximate structure in $P \overline{1}$. The results were expressed in the form of the angles made by the molecular long axis with the $z$ axis of the cell and the positions of the atoms in the subcell. Atomic coordinates were not explicitly given and although two somewhat poorly resolved Fourier projections were published no observed or calculated structure factors were given. It is clear that any structural inferences drawn from Kitaigorodsky \& Mnyukh's work would of necessity be very approximate.

Hayashida (1962) published a paper on the crystal structure of octadecane based on photometrically measured intensity data from the $h 0 l$ and $0 k l$ zones. (In addition, hhl data were said to have been collected but these were not published). The cell constants given by Hayashida differed from those given by M \& L (Table 1) but, according to him, 'agreed well. . . after a transformation of axes'. Hayashida also claimed that his cell volume agreed with that given by M \& L which it manifestly did not, M \& L giving explicitly $454 \cdot 4 \AA$ Hayashida giving $398 \cdot 1 \AA^{3}$. (This is in any

[^0]case wrong; the cell given by Hayashida would have a volume $436 \cdot 2 \AA^{3}$.) Hayashida made no reference to the work of Kitaigorodsky \& Mnyukh.

In 1970, Crissman, Passaglia, Eby \& Colson measured the positions of the powder lines of the next triclinic $n$-even homologue, eicosane, $\mathrm{C}_{20} \mathrm{H}_{42}$. They showed, as might be expected, that five of the six cell parameters were virtually identical to those given by $\mathrm{M} \& \mathrm{~L}$ for octadecane (II, Table 1). The $c$ repeat is longer by $2.45 \AA$ to accommodate the two extra methylene groups. In a footnote, Crissman et al. remarked that for $\mathrm{C}_{18} \mathrm{H}_{38}$ neither $d(001)$ nor the cell volume given by Hayashida agreed with those given by M \& L.

We first became concerned about the structure of $\mathrm{C}_{18} \mathrm{H}_{38}$ published by Hayashida when we discovered that the triclinic cell would not yield the same Delauney reduced cell as that given by M \& L (already reduced). We also found that the atomic coordinates given by Hayashida gave $\mathrm{C}-\mathrm{C}$ bond lengths alternating between 1.38 and $1.70 \AA$. That there was a discrepancy between the cells given by M \& L and by Hayashida was also noted by an Editor of Structure Reports (1962) in which the $\beta$ angle given by Hayashida is changed to its supplement. We found that this modified cell does indeed reduce reasonably well to the cell given by $\mathrm{M} \& \mathrm{~L}$ but the atomic coordinates are still wrong.

We have traced the error to Hayashida's faulty assignment of the $\gamma$ cell angle, which in turn seems to have arisen from a misindexing of the 0 kl reflexions as $0 k \bar{l}$. (We have confirmed this on a precession photograph of $\mathrm{C}_{20} \mathrm{H}_{42}$ ). Unfortunately $\gamma$ was not consistently mis-assigned. Thus the $h 0 l$ projection has the correct $\pi-\beta^{*}$ angle (II, Table 2) between $x$ and $z$ axes. Both $0 k l$ projections [Hayashida (1962), Figs. 1(b) and 3] have the correct $\pi-\alpha^{*}$ angle between axes but the former has $y$ running in the wrong direction. In contrast the $h k 0$ projection has quite the wrong angle between axes. It has been calculated from the erroneous $\gamma$ instead of from its supplement.

Table 1. Real-cell dimensions for $\mathrm{C}_{18} \mathrm{H}_{38}$ (except II which is $\mathrm{C}_{20} \mathrm{H}_{42}$ )

|  | $a$ | $b$ | $c$ | $\alpha$ | $\beta$ | $\gamma$ |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: |
| II | $4.285 \AA$ | $4.820 \AA$ | $23.070 \AA$ | $91 \cdot 10^{\circ}$ | $92.07^{\circ}$ | $107 \cdot 30^{\circ}$ |
| II | 4.281 | 4.821 | $(25.52)$ | $91 \cdot 18$ | 93.52 | 107.35 |
| III | 4.361 | 4.893 | 23.08 | 90.43 | 92.87 | 111.40 |
| IV | 4.361 | 4.893 | 25.04 | $83 \cdot 10$ | 67.07 | 68.60 |
| V | 4.285 | 4.820 | 24.898 | $85 \cdot 15$ | 67.80 | 72.70 |

I Müller \& Lonsdale (1948).
II Crissman et al. (1970).
III Hayashida (1962) with $\gamma$ changed to supplement and after Delauney reduction.
IV Hayashida (1962) with $y$ changed to supplement.
V Müller \& Lonsdale (1948) after transformation to axial system IV.

We have now corrected Hayashida's error and refined the structure using his intensity data. Refinement was carried out first changing $\gamma$ to its supplement together with the following changes:
(i) all 0 kl changed to $0 k \bar{l}$,
(ii) the centre of the molecule was moved to the origin of coordinates,
(iii) $y$ coordinates for carbon reversed from those given by Hayashida,
(iv) hydrogen coordinates calculated from the revised carbon coordinates taking $\mathrm{C}-\mathrm{H}$ as $1 \cdot 07_{5} \AA$ and tetrahedral $\mathrm{H}-\mathrm{C}-\mathrm{H}$ angle. Terminal hydrogen atoms were assumed to lie in the plane of the molecule.

Full-matrix least-squares refinement was first carried out with isotropic temperature factors on the carbon atoms. This gave good results so that the hydrogen positions were recalculated and an anisotropic refinement carried out on the carbon atoms keeping all hydrogen atoms fixed with $B=5 \cdot 0 \AA^{2}$. (The $\beta_{12}$ factor for the carbon atoms could not be refined owing to the absence of $h k 0$ and $h k l$ data. Accordingly, these parameters were kept fixed at the values derived from the $B$ factors obtained in the first refinement.) The conventional $R$ index at the end of refinement was $8 \%$. The observed (Hayashida) and calculated structure factors are given in Table 3, the atomic coordinates and

Table 2. Reciprocal cell dimensions for $\mathrm{C}_{18} \mathrm{H}_{38}$

|  | $a^{*}$ | $b^{*}$ | $c^{*}$ | $\alpha^{*}$ | $\beta^{*}$ | $\gamma^{*}$ |
| ---: | :--- | :--- | :--- | :---: | :---: | :---: |
| I | $0.2788 \AA^{-1}$ | $0.2306 \AA-1$ | $0.0455 \AA-1$ | $107.81^{\circ}$ | $117.97^{\circ}$ | $62.24^{\circ}$ |
| II | 0.2656 | 0.2196 | 0.0434 | 88.53 | 111.97 | 110.36 |
| III | 0.2632 | 0.2174 | 0.0434 | 88.20 | 111.76 | 106.72 |

I Hayashida (1962) with $\gamma=111 \cdot 40^{\circ}$, as published.
II Hayashida (1962) with $\gamma=68 \cdot 60^{\circ}$.
III Müller \& Lonsdale (1948, V, Table 1).

Table 3. Structure factors $\left|F_{o}\right| \times 10$ (after Hayashida) and $F_{c} \times 10$


Table 4. Fractional coordinates $\times 10^{3}(x$ and $y), \times 10^{4}(z)$ and anisotropic temperature factors $\times 10^{3}\left(\beta_{11}, \beta_{22}, \beta_{12}\right)$, $\times 10^{4}\left(\beta_{33}, \beta_{13}, \beta_{33}\right)$ for carbon atoms

$$
\text { T.F. }=\exp \left[-\left(\beta_{11} h^{2}+\beta_{22} k^{2}+\beta_{33} /^{2}+2 \beta_{12} h k+2 \beta_{13} h l+2 \beta_{23} k l\right)\right] .
$$

$C(1)$
$C(2)$
$C(3)$
$C(4)$
$C(5)$
$C(6)$
$C(7)$
$C(8)$
$C(9)$

| $x$ | $y$ | $z$ | $\beta_{11}$ | $\beta_{22}$ | $\beta_{33}$ | $\beta_{12} \dagger$ | $\beta_{13}$ | $\beta_{23}$ |
| ---: | ---: | :---: | :---: | :---: | :---: | :---: | ---: | ---: |
| 80 | 273 | -4401 | 157 | 91 | 31 | -36 | -103 | -1 |
| 141 | 77 | -3932 | 172 | 77 | 23 | -29 | -116 | 0 |
| 57 | 230 | -3372 | 131 | 55 | 27 | -27 | -95 | 1 |
| 112 | 35 | -2892 | 124 | 60 | 23 | -26 | -76 | -1 |
| 33 | 189 | -2328 | 114 | 54 | 23 | -25 | -68 | 1 |
| 83 | -10 | -1845 | 114 | 57 | 24 | -25 | -86 | 1 |
| 6 | 143 | -1285 | 107 | 52 | 23 | -24 | -74 | 0 |
| 53 | -56 | -802 | 103 | 46 | 23 | -23 | -74 | 1 |
| -21 | 101 | -245 | 96 | 53 | 25 | -24 | -76 | 1 |

temperature factors for carbon in Table 4 and derived hydrogen coordinates in Table 5.

Table 5. Derived hydrogen fractional coordinates, $\times 10^{3}(x$ and $y), \times 10^{4}(z)$

|  | $x$ | $y$ | $z$ |
| :--- | ---: | ---: | ---: |
| H2(1) | 243 | 419 | -4498 |
| H2(2) | -20 | -66 | -3847 |
| H2(3) | 220 | 371 | -3459 |
| H2(4) | -54 | -104 | -2801 |
| H2(5) | 203 | 324 | -2416 |
| H2(6) | -87 | -145 | -1756 |
| H2(7) | 178 | 277 | -1373 |
| H2(8) | -123 | -187 | -709 |
| H2(9) | 157 | 229 | -337 |
| H3(1) | -188 | 396 | -4263 |
| H3(2) | 412 | -46 | -4085 |
| H3(3) | -214 | 356 | -3223 |
| H34 | 382 | -94 | -3043 |
| H3(5) | -235 | 321 | -2180 |
| H3(6) | 351 | -143 | -1994 |
| H3(7) | -261 | 279 | -1139 |
| H38 | 318 | -193 | -950 |
| H3(9) | -286 | 240 | -100 |
| H1(1) | 153 | 145 | -4784 |

The calculated bond lengths and angles were reasonably good but showed some alternation in magnitude along the molecular chain. We have now traced this to what we believe to be the inaccurate cell parameters used by Hayashida. Table 1 shows that the cell parameters given by $M \& L$ for $\mathrm{C}_{18} \mathrm{H}_{38}$ and those given by Crissman et al. (1970) for $\mathrm{C}_{20} \mathrm{H}_{42}$ agree better with each other (apart from $\beta$ ) than with the parameters obtained from Hayashida's cell after reduction. Accordingly, we have used the M \& L parameters transformed to the system used by Hayashida (V, Table 1). Use of cell parameters removed the apparent alternation in bond lengths and angles along the chain. The results, which are of unknown accuracy, but probably of order $0.05 \AA$ and $2^{\circ}$ are given in Table 6.

Table 6. $\mathrm{C}-\mathrm{C}$ bond lengths and $\mathrm{C}-\mathrm{C}-\mathrm{C}$ angles

| $\mathrm{C}(1)-\mathrm{C}(2)$ | $1 \cdot 49 \AA$ | $\mathrm{C}(1)-\mathrm{C}(2)-\mathrm{C}(3)$ | $114 \cdot 9^{\circ}$ |
| :--- | :--- | :--- | :--- |
| $\mathrm{C}(2)-\mathrm{C}(3)$ | $1 \cdot 50$ | $\mathrm{C}(2)-\mathrm{C}(3)-\mathrm{C}(4)$ | $115 \cdot 5$ |
| $\mathrm{C}(3)-\mathrm{C}(4)$ | $1 \cdot 50$ | $\mathrm{C}(3)-\mathrm{C}(4)-\mathrm{C}(5)$ | $115 \cdot 6$ |
| $\mathrm{C}(4)-\mathrm{C}(5)$ | $1 \cdot 52$ | $\mathrm{C}(4)-\mathrm{C}(5)-\mathrm{C}(6)$ | $115 \cdot 0$ |
| $\mathrm{C}(5)-\mathrm{C}(6)$ | $1 \cdot 51$ | $\mathrm{C}(5)-\mathrm{C}(6)-\mathrm{C}(7)$ | $115 \cdot 0$ |
| $\mathrm{C}(6)-\mathrm{C}(7)$ | $1 \cdot 51$ | $\mathrm{C}(6)-\mathrm{C}(7)-\mathrm{C}(8)$ | $114 \cdot 8$ |
| $\mathrm{C}(7)-\mathrm{C}(8)$ | $1 \cdot 51$ | $\mathrm{C}(7)-\mathrm{C}(8)-\mathrm{C}(9)$ | $114 \cdot 3$ |
| $\mathrm{C}(8)-\mathrm{C}(9)$ | 1.52 | $\mathrm{C}(8)-\mathrm{C}(9)-\mathrm{C}\left(9^{\prime}\right)$ | $114 \cdot 2$ |
| $\mathrm{C}(9)-\mathrm{C}\left(9^{\prime}\right)$ | 1.52 |  |  |

The $\mathrm{C}-\mathrm{C}$ bonds are somewhat shorter and the $\mathrm{C}-\mathrm{C}-\mathrm{C}$ angles somewhat larger than those found in n-alkanes generally. The lower members, whose structures are more accurately known, give typically 1.533 (6) $\AA$ and $112 \cdot 1$ (3) ${ }^{\circ}$ (for pentane, see Mathisen, Norman \& Pedersen, 1967). The results obtained here may well be due to the marked librational motion of the carbon atoms in planes normal to the chain axis. This is well illustrated by the ORTEP plot Fig. 1 which shows a
steady increase in size of the thermal ellipsoids as one moves outwards from the centre of the molecule. This would have the well known effect of bringing the mean positions of the carbon atoms inwards towards the chain axis thus shortening the $\mathrm{C}-\mathrm{C}$ bonds and widening the $\mathrm{C}-\mathrm{C}-\mathrm{C}$ angles.

## Packing

The shortest non-bonded contacts are all $\mathrm{H} \cdots \mathrm{H}$. Fig. 2 shows the central parts of the molecules in $z$ projection and, because the molecules are parallel to each other, the diagram is typical of those for any other sets of carbon atoms along the chain. (The only change is a movement away from the origin of coordinates because the molecular axis is not parallel to the $z$ axis.)


Fig. 1. ORTEP plot of half-molecule in $y$ projection.


Fig. 2. Close contacts illustrated for molecular centre in $z$ projection.


Fig. 3. Close contacts at ends of molecules ( $y$ projection).

The centre of symmetry at the molecular midpoint is between atoms $\mathbf{C}(9)$ and $\mathbf{C}\left(9^{\prime}\right)$, Fig. 2. The shortest $\mathrm{H} \cdots \mathrm{H}$ distances between adjacent chains are of five kinds and are very closely similar in length. Atom $\mathrm{H} 2(9)$ lies $p=2.68 \AA$ from $\mathrm{H} 3(9)$ and $s=2 \cdot 60 \AA$ from H3(7). The distances $p$ and $s$ for the whole chain range between $2.67_{8}$ and $2.68{ }_{4} \AA$ and 2.57 and $2.61 \AA$ respectively. Because of the centre of symmetry at the molecular midpoint $\mathrm{H} 2\left(7^{\prime}\right), \mathrm{H} 2\left(9^{\prime}\right)$ are related in the same way. However, if we move down the chain towards $\mathrm{C}(1)$,
the hydrogen atoms lying beneath $\mathrm{H} 2\left(9^{\prime}\right)$ and $\mathrm{H} 3\left(9^{\prime}\right)$ are all attached to even-numbered carbon atoms. These hydrogen atoms show similar non-bonded distances to those on neighbouring chains. Thus distance $r$, typified by $\mathrm{H} 2(8)-\mathrm{H} 3(8)$, is $2.69 \AA$ and $t$, typified by $\mathrm{H} 2(8)-\mathrm{H} 3\left(9^{\prime}\right)$, is $2.64 \AA$. The distances $r$ range between 2.68 and $2.69 \AA$, distances $t$ between 2.62 and $2.64 \AA$.

The fifth type of close contact between adjacent chains is $q$, typified by H3(9)-H3(9'), $2 \cdot 59 \AA$. These $q$ distances range between the latter value and $2 \cdot 69 \AA$.

There are three types of $\mathrm{H} \cdots \mathrm{H}$ contact between the ends of the chains. Two of these of length $2 \cdot 68$ and $2.73 \AA$ are between $\mathrm{Hl}(1)$ terminal hydrogen atoms and the other of length $2.71 \AA$ is between $\mathrm{Hl}(1)$ of one chain and H3(2) of another (Fig. 3).

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## References

Broadhurst, M. G. (1962). J. Res. Natl. Bur. Stand. 66A, 241.

Crissman, J. M., Passaglia, E., Eby, R. K. \& Colson, J. P. (1970). J. Appl. Cryst. 3, 194.

Hayashida, T. (1962). J. Phys. Soc. Japan, 17, 306.
Kitaigorodsky, A. K. \& Mnyukh, Yu. V., (1969). Izv. Akad. Nauk SSSR, Otd. Khim. Nauk, p. 2088.
Mathisen, H., Norman, N. \& Pedersen, B. F. (1967). Acta Chem. Scand. 21, 127.
Müller, A. \& Lonsdale, K. (1948). Acta Cryst. 1, 129.
Smith, A. E. (1953). J. Chem. Phys. 21, 2229.
Structure Reports (1962). Vol. 27, p. 743. Utrecht: Oosthoek.

# A Neutron Diffraction Study of the Anisotropic Thermal Expansion of $\boldsymbol{\beta}$-Uranyl Dihydroxide 

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Neutron diffraction powder patterns were taken to obtain positional parameters for all the atoms in $\beta-\mathrm{UO}_{2}(\mathrm{OH})_{2}$ at six temperatures from 21 to $260^{\circ} \mathrm{C}$. The results confirm that the strongly anisotropic thermal expansion of this material is caused by the rotation of oxygen octahedra in the structure. These octahedra also undergo temperature-induced shape changes, which may be attributed to the effects of hydrogen bonding in the structure.

## Introduction

In a previous publication (Bannister \& Taylor, 1970), it was shown that the thermal expansion of $\beta-\mathrm{UO}_{2}(\mathrm{OH})_{2}$ is anisotropic, with a large contraction in $a$, a large expansion in $b$ and a smaller cyclic change in $c$. The anisotropy reaches a saturation level at $260^{\circ} \mathrm{C}$. It was
proposed that the effect is caused by a rotation of the $\mathrm{U}-\mathrm{O}(2)$ (hydroxyl oxygen) bonds about [110], their inclination to that direction being unchanged. At saturation, the $\mathrm{O}(2)$ atoms reach their maximum possible intrusion into holes in the structure, and the $\mathrm{O}(2)$ plane of the oxygen octahedra surrounding each uranium atom has its maximum tilt with respect to the (001)


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